



OPEN

SUBJECT AREAS:
BIOLOGICAL PHYSICS
STATISTICAL PHYSICS
THERMODYNAMICSReceived
13 June 2014Accepted
20 October 2014Published
12 November 2014Correspondence and
requests for materials
should be addressed to
R.R. (roland.roth@uni-
tuebingen.de)

Ion-activated attractive patches as a mechanism for controlled protein interactions

Felix Roosen-Runge^{1,2}, Fajun Zhang¹, Frank Schreiber¹ & Roland Roth³¹Institut für Angewandte Physik, Universität Tübingen, Auf der Morgenstelle 10, 72076 Tübingen, Germany, ²Institut Laue-Langevin, 71 avenue des Martyrs, 38042 Grenoble, France, ³Institut für Theoretische Physik, Universität Tübingen, Auf der Morgenstelle 14, 72076 Tübingen, Germany.

The understanding of protein interactions to control phase and nucleation behavior of protein solutions is an important challenge for soft matter, biological and medical research. Here, we present ion bridges of multivalent cations between proteins as an *ion-activated* mechanism for patchy interaction that is directly supported by experimental findings in protein crystals. A deep understanding of experimentally observed phenomena in protein solutions—including charge reversal, reentrant condensation, metastable liquid-liquid phase separation, cluster formation and different pathways of crystallization—is gained by an analytic model that directly displays parameter dependencies and physical connections. The direct connection between experiment and theory provides a conceptual framework for future experimental, computational and theoretical research on topics such as rational design of phase behavior and crystallization pathways on the basis of the statistical physics of patchy particles.

Patchy particles represent elegant models to explore the statistical physics of soft matter systems with directional interactions, in particular via the Wertheim theory for associating fluids^{1–6}. Exploiting different choices of the patch-patch interaction, novel phenomena such as empty liquids⁷, reentrant network formation⁸ and control of crystallization pathways^{9,10} have been found in calculations and simulations. In several theoretical studies, patchy particles have been suggested to be a model system for proteins^{9–15}. So far the connection between patchy particles and proteins has been based on general considerations concerning the non-spherical shape and inhomogeneous surface patterns of charge and hydrophobicity, as well as on indirect indications such as low density crystals and low critical volume fractions¹⁶. Furthermore, single point mutations in the protein sequence have been found to induce significant differences in the phase behavior, suggesting that local variations at the protein surface can change the interaction strongly^{17–19}. Recently, a computational study used crystal structures of four mutants of one protein to parametrize a patchy model that successfully reproduced the experimental variation of the phase behavior of the mutants¹⁹. These findings demonstrate that the framework of patchy particles is appropriate for proteins. Nevertheless, exploiting the full power of the conceptual framework of patchy particles for control of experimental phase behavior of protein solutions depends on identifying experimental ways to control interaction patches at the protein surface.

Here we present a mechanism for *ion-activated* attractive patches between proteins that is directly supported by experimental evidence. Our model introduces a novel analytical concept how to account for ion-induced protein interactions by explicitly modeling the role of the cations. This concept can be seamlessly employed in both theory and simulations of patchy particles. Here we use the well-established analytical theory due to Wertheim^{1–6} in order to highlight the essential physics that drives the interesting and rich phenomenology in protein solutions in the presence of multivalent cations.

Multivalent metal cations such as Yttrium(III) form multidentate coordinative bonds with solvent-exposed carboxylic side chains on the protein surface^{20,21}. For globular proteins with negative charge, ion binding is experimentally reflected in a charge inversion of the protein net charge upon the addition of YCl₃ (Fig. 1A)^{22,23}. Importantly, multivalent cations cross-link protein molecules in crystals (Fig. 1B)²⁴. These ion bridges represent attractive patches that are activated by cations, and can be employed to tune the interactions and the associated phase behavior of globular proteins. Since solvent-exposed carboxylic side chains are ubiquitous in globular proteins, the presented mechanism applies to a large part of the protein family²⁵. Thus, while the control of other interaction patches through e.g. surface patterns of hydrophobicity or charge requires rather involved

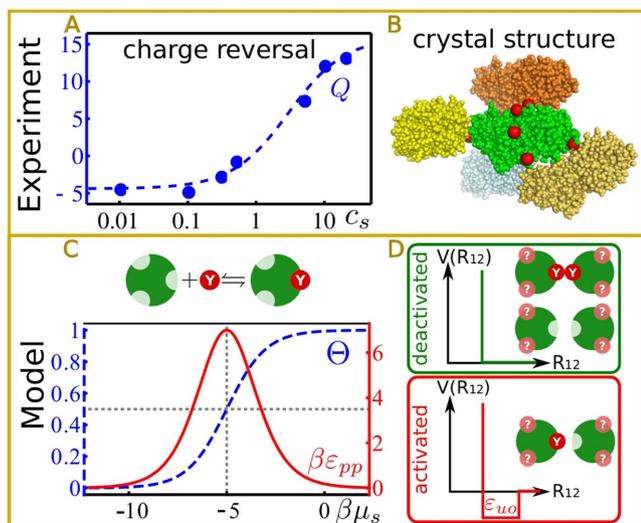


Figure 1 | Ion binding and ion bridging govern the protein interaction. Experimental observations: (A): Multivalent cations (here: YCl_3 , c_s in mM) cause a charge reversal in protein solutions (here: HSA 5 g/l), evidencing ion binding. The surface charges were obtained as described in Ref. 23. The dashed line corresponds to a Langmuir isotherm (see Methods). (B): In protein crystal structures (here: β -lactoglobulin dimers with Y^{3+} , PDB 3PH6²⁴), neighboring molecules are cross-linked by bridges of multivalent ions. For clarity, only 4 of 8 neighboring dimers are shown. Protein model with ion-activated attractive patches: (C + D): The average occupancy Θ (Eq. (3)) reflects the charge reversal. From the ion-bridge energy ε_{u0} and the probability for an occupied and unoccupied patch to meet, the ion-induced patch-patch attraction strength ε_{pp} (Eq. (5)) results as a non-monotonous function of the chemical potential μ_s that represents the concentration of free cations.

biotechnological methods such as genetic engineering and structure prediction, the addition of cations allows for activation of patches via a comparatively simple physicochemical experimental procedure.

This mechanism for ion-activated protein interaction is of special interest in the context of phase behavior of protein solutions. In general, additives such as NaCl or PEG are known to induce liquid-liquid phase separation (LLPS)^{13,26–31} and solvent-controlled crystallization pathways^{32,33}. Equilibrium clusters have been found in lysozyme solutions³⁴ as expected for charged and attractive colloids^{35,36} and attractive fluids in general^{37,38}. In these cases, the results are usually discussed invoking unspecific effects such as screened Coulomb interaction or depletion effects. Here, we focus on the addition of trivalent cations that allows via a specific mechanism to control the protein interactions. Trivalent salts such as YCl_3 have been found to induce a rich experimental phenomenology in solutions of globular proteins, including reentrant condensation, LLPS (Fig. 2A), cluster phases, and one-step as well as two-step pathways of protein crystallization^{22,24,39,40}. Using our analytical model of ion-activated attractive patches by bridges of multivalent cations, the rich phenomenology is explained and understood in a very natural way (Fig. 2B), demonstrating that the concept of ion-activated patches provides a novel and very powerful framework to control the experimental phase behavior of protein solutions. This study introduces the basic mechanism using comparisons to experimental results in protein solutions with YCl_3 . We emphasize that for a quantitative modeling further effects such as pH variation and electrostatics have to be accounted for explicitly. Although Y^{3+} is no biologically active cation, the study presents relevant results for the understanding of protein solutions. First, similar results are obtained for several tri- and divalent cations²³ such as the biologically active cations Fe^{3+} and Al^{3+} , implying that ion bridges indeed present a general

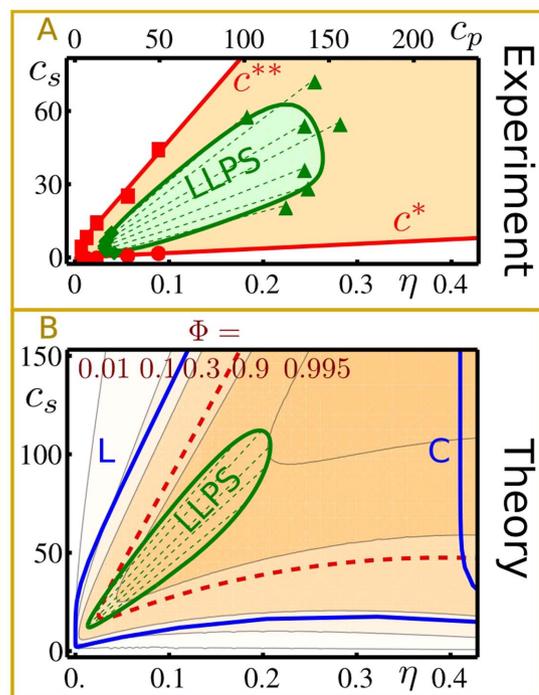


Figure 2 | Phase behavior of protein solutions with multivalent cations that activate attractive patches on the protein surface. (A): The isothermal phase diagram from experiment (here: HSA with YCl_3 , replotted from Ref. 39) shows a reentrant condensation for $c^* < c_s < c^{**}$ and a homogeneous solution otherwise. In the condensed regime, a metastable LLPS is observed. (B): The phase diagram based on the presented model accounts for all experimental observations. The closed LLPS region is indicated as green area. The cluster fraction Φ is shown as orange contour plot, respectively. The connection to the reentrant condensation and physical implications of percolation (red dashed line) are discussed in the text.

mechanism. Second, the possibility to activate attractive protein interactions by multivalent cations provides control on phase behavior and pathways of nucleation and crystallization, which is of importance for structural biology as well as an understanding of self-assembly in protein solutions.

Analytical Model for the Activation of Attractive Patches

Within our analytical approach proteins are modeled as particles with m patches per particle. Multivalent cations are modeled as bridge particles, which can bind to a patch and thereby activate it. Other ions are not considered here. The interaction between proteins is given by the hard sphere repulsion V_{HS} between the particles and square-well attractions between the patches¹:

$$V(1,2) = V_{HS}(R_{12}) + \sum_{i=1}^m \sum_{j=1}^m V_{pp}(r_{12}^{ij}), \quad (1)$$

$$V_{pp}(r_{12}^{ij}) = \begin{cases} -\varepsilon_{pp} & \text{for } r_{12}^{ij} < r_c \\ 0 & \text{for } r_c \leq r_{12}^{ij}. \end{cases} \quad (2)$$

R_{12} denotes the center-to-center distance of the particles. r_{12}^{ij} is the distance between the centers of patch i of particle 1 and patch j of particle 2.

The key point of our model is the fact that ion binding controls the attraction strength ε_{pp} , thereby representing the activation of interaction patches. The binding sites are considered as independent from each other with binding energy ε_b . Since a binding site can either be



unoccupied (u), or occupied (o) by at most one cation, the average occupancy Θ of each binding site is given by the statistics of a two-state system in the grand canonical ensemble:

$$\Theta = \frac{1}{\exp(\beta(\varepsilon_b - \mu_s)) + 1}, \quad (3)$$

with $\beta = (k_B T)^{-1}$. The chemical potential μ_s of the salt (s) cations sets the reservoir concentration c_s^r . For the concentrations used in the experiments we can approximate this relation via $c_s^r(\mu_s) \approx \rho_0 \exp(\beta\mu_s)$. Note that possible non-idealities of the salt bulk solution do not change the resulting phase behavior qualitatively, but only slightly rescale the relation $c_s^r(\mu_s)$. We have obtained a comparable behavior for numerical calculations of charged hard spheres, but prefer to use the analytic form of Eq. (3) to allow for an analytic and understandable model focusing on the mechanism of ion-bridging.

The patch-patch interaction energy ε_{pp} is determined from three contributions (see Fig. 1C,D) depending on the average occupancy Θ of two interacting patches:

$$\varepsilon_{pp} = \varepsilon_{uu}(1 - \Theta)^2 + 2\varepsilon_{uo}\Theta(1 - \Theta) + \varepsilon_{oo}\Theta^2. \quad (4)$$

The first term accounts for the interaction between two unoccupied patches, which meet with a probability of $(1 - \Theta)^2$. The second term represents the ion-bridge attraction, when an unoccupied and an occupied patch become cross-linked, with a probability of $2\Theta(1 - \Theta)$. The third term describes the interaction between two occupied patches, with a probability of Θ^2 . In order to recover hard-sphere interaction for fully occupied or unoccupied patches, we choose $\varepsilon_{uu} = \varepsilon_{oo} = 0$. Then ε_{pp} reads

$$\beta\varepsilon_{pp} = \frac{2\beta\varepsilon_{uo}\exp(\beta\varepsilon_b - \beta\mu_s)}{(\exp(\beta\varepsilon_b - \beta\mu_s) + 1)^2}. \quad (5)$$

Eq. (5) contains the essential physics of our model: the binding energy ε_b relates to the effective patch-patch attraction strength ε_{pp} , thereby expressing the activation of patches with fixed attraction ε_{uo} . While the model suggests a clear physical picture of cation binding at specific surface sites and cation bridges, the physical origin of ε_b and ε_{uo} is of minor importance within this framework. In particular, electrostatic contributions and ion-ion correlations between the multivalent cations as well as coordinative binding of metal ions to surface groups can contribute to the energies.

The experimental control parameter is the total salt concentration c_s in the system, which is the sum of the ions bound at the surfaces and the free ions in solution. In the model it is more convenient to use the salt concentration in the reservoir c_s^r as control variable. The connection between these two quantities is given by

$$c_s = m\Theta\rho + c_s^r(\mu_s)\left(1 - \eta(1 + R_s/R_p)^3\right), \quad (6)$$

where R_s and R_p are the (effective) radii of salt ions and proteins, respectively. The first term accounts for the ions bound to proteins. The second term originates from the free ions in the solution, corrected for the volume excluded to ions⁴¹. The number density ρ is related to the protein volume fraction $\eta = \frac{4}{3}\pi R_p^3\rho$.

The outlined novel concept to account for the attractive interactions due to ion-bridges can be embedded seamlessly into the Wertheim theory of patchy particles (see Methods). The liquid-liquid and solid-liquid phase coexistence at temperature T follows from chemical and mechanical equilibrium, $\mu_1 = \mu_2$ and $P_1 = P_2$, respectively, between phases 1 and 2. The chemical potential $\mu = \partial f / \partial \rho|_{VT}$, pressure $P = \rho\mu - f$, and isothermal compressibility $\chi_T = 1/\rho(\partial P / \partial \rho)^{-1}$ are calculated analytically from the free energy densities f of the solid and fluid phase (for further details, see Methods).

As an alternative approach within the Wertheim theory, the proteins could be modeled as particles with two dissimilar types of

patches – patch type A , if the binding site is unoccupied, and patch type B , if it is occupied. In this case, the average occupancy Θ , Eq. (3), would control the numbers of A and B patches. The protein-protein attraction ε_{pp} , Eq. (5), would be generated by the Wertheim theory, for a given interaction between A and B patches of $\varepsilon_{AB} = \varepsilon_{uo}$. We have verified that, while this approach is numerically and theoretically somewhat more involved, it results in equivalent behavior for our system. By presenting the model more explicitly in Eqs. (5)–(6) we wish to highlight the underlying physics of the ion-activated protein interactions.

Model Analysis and Discussion

The main feature of our model is the formation of ion bridges: If an occupied patch interacts with an unoccupied patch, an ion bridge forms and links the participating proteins (Fig. 1D). Based on the attractive interaction induced by the ion bridges, several phenomena in the system become intuitively clear. At low ion concentrations ($\Theta \rightarrow 0$) the proteins repel each other – in the model by the hard-sphere interaction and in the experimental system through electrostatic repulsion. As more ions are added to the system more binding sites become occupied, i.e. Θ increases, which in the experimental system results in a reduced net charge (Fig. 1A,C). For $\Theta < 0.5$ the addition of ions increases the attraction between proteins, since the probability for an occupied and an unoccupied patch to meet increases. Further increasing the ion concentration ($\Theta > 0.5$) decreases the attraction since too many binding sites are already occupied, thereby reflecting the charge reversal (Fig. 1A,C). At high enough ion concentration, the probability for ion-bridge formation is low and proteins mainly repel each other, corresponding to the reentrant homogeneous phase.

If the attraction is sufficiently strong and the protein volume fraction η is in the right range, a LLPS occurs in a closed area (green line in Fig. 2). Importantly, the low volume fractions of the coexistent liquid phases can be understood with patchy particles, which is not possible using only isotropic potentials⁴². As expected for protein solutions, the LLPS is found to be metastable with respect to a crystal phase (blue line in Fig. 2B). We find excellent agreement between theory and experiment (Fig. 2).

A natural consequence of the ion bridges is the formation of clusters throughout the entire phase diagram (Fig. 2B). Using the Flory-Stockmeyer theory^{43,44} the number density ρ_n of n -clusters and the number fraction Φ of proteins in clusters are given by

$$\rho_n = \rho(1 - p_b)^m [p_b(1 - p_b)^{m-2}]^{n-1} \frac{m(mn - n)!}{(mn - 2n + 2)!n!}, \quad (7)$$

$$\Phi = \frac{\rho - \rho_1}{\rho} = 1 - (1 - p_b)^m. \quad (8)$$

With increasing average ion-bridge probability p_b , which is provided by the Wertheim theory¹ (see Methods), larger cluster become more frequent (Fig. 3A). Thus, with increasing p_b , protein diffusion is expected to be reduced substantially due to cluster formation, as indeed observed in recent experiments⁴⁵. Once p_b exceeds the percolation value $p_b^* = 1/(m - 1)$, a system-spanning cluster can form, implying that dynamics in the solution is severely slowed down or even arrested.

The formation of clusters provides an explanation for the experimentally observed turbidity in the condensed regime in the concentration range between the boundaries c^* and c^{**} (red lines in Fig. 2A). Using the approximation of Rayleigh scattering, the scattering of n -clusters grows with $V^2 \propto n^2$, which causes a steep increase of the integrated scattering power $I_c = \sum_{n=1}^{\infty} n^2 \rho_n$ with increasing p_b , in particular when approaching the percolation threshold p_b^* (Fig. 3B). In addition, as the liquid-liquid phase boundary is approached, opalescence causes turbidity in the solution, being man-

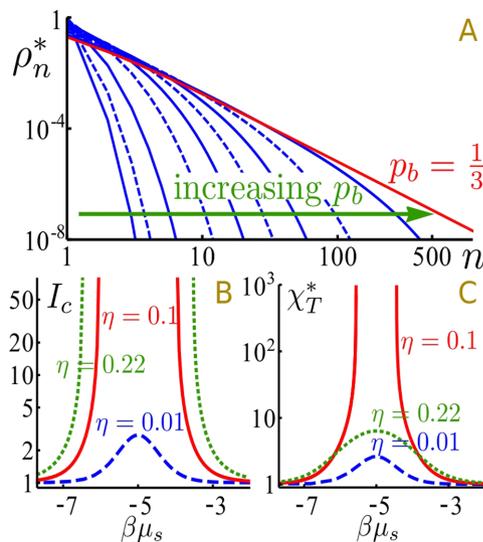


Figure 3 | (A): The cluster size distribution $\rho_n^* = \rho_n/\rho$ broadens with increasing bond probability (blue lines: $p_b = 0.0001, 0.001, 0.01, 0.05, 0.1, 0.15, 0.2, 0.25, 0.3$; red line: $p_b = p_b^* = 1/3$), implying the growth of larger clusters, in particular when approaching the percolation limit p_b^* . (B): The integrated scattering power of all clusters, normalized to the monomer solution, shows a steep increase at intermediate chemical potentials μ_s , i.e. intermediate salt concentrations. This behavior represents one reason for the turbidity in the solution during the reentrant condensation. (C): Another reason for turbidity is opalescence close to the LLPS boundary and the LLPS itself. The forward scattering intensity is proportional to the isothermal compressibility $\chi_T^* = \chi_T/\chi_T^{HS}$, normalized to the hard sphere value, that outlines the reentrant effect. The calculations in B, C are performed for three volume fractions below, through and above the LLPS.

ifested in the increase of the isothermal compressibility of the patchy particle solution (Fig. 3C).

In protein solutions with multivalent cations, crystals are found experimentally to grow from the dilute phase after LLPS^{39,40}, whereas crystal nucleation should be more favorable in the dense phase according to classical nucleation theory. Although crystallization pathways of patchy particles depends also on dynamical aspects¹⁴, two thermodynamic features of our model help to rationalize the experimental observations. First, the dense phase occurs beyond the percolation line and, thus, might be an arrested phase, implying that motions necessary to rearrange from disordered clusters to ordered crystals might be hindered. Second, a considerable amount of clusters is present around the dilute coexistence boundary (Fig. 2B). These clusters might act as precursors in two-step nucleation pathways that occur much faster than the classical one-step nucleation from homogeneous solution⁴⁰.

The presented framework focuses on the basic understanding of the phenomenology of the ion-bridging mechanism, and therefore models the complex experimental system by its essential features in an analytical and accessible description using the Wertheim theory. The analytic approach allows not only to describe but also to *understand* the phenomena observed in solutions of protein and salt. The mechanism of cation-activated attractive patches can be seamlessly embedded in more detailed theoretical studies and simulations to address multiple questions beyond the present study. First, electrostatics are accounted for in our framework only implicitly by the choice of the effective interaction. Including electrostatics explicitly, the effect of long-ranged repulsion on cluster formation and gelation³⁶ as well as crystallization pathways could be studied. Second, cation–cation correlations as well as dynamical aspects affecting the patch occupation are neglected in the present mean-field equilibrium

picture, since the large binding energy of the cations dominates the cation–protein interaction, and thus the ion bridging²⁵. However, cation–cation correlations could provide relevant information on e.g. the dynamics and the detailed pathways of protein crystallization^{10,14}. Third, the effect of the geometry of the patch arrangement is not accounted for by the Wertheim theory and is only included implicitly by the choice of the crystal volume fraction (see Methods). An analysis of the ion-bridge mechanism extended towards inhomogeneous patch occupations would be very interesting for a detailed description of the dense and solid phase as well as crystal polymorphs^{10,24}. The presented mechanism thus is the basis for detailed theoretical predictions, and presents promising opportunities not only for the study of the protein systems, but also for the general understanding of charged soft matter.

Conclusions

We have presented an experimentally supported mechanism of cation bridges between neighboring molecules as a method to activate attractive patches at the protein surface. This mechanism provides a comprehensive understanding of the experimental observations in protein solutions, and allows validation and application of patchy particle models in real protein solutions. The cation concentration represents an independent control parameter, promising rational design and control of phase behavior of protein solutions using multivalent cations and the statistical physics of particles with ion-activated patches. Our model provides a natural analytical connection between experimental results of protein biophysics and the study of patchy particles within the framework of theory and simulations. A natural next step is to extend our model to inhomogeneous density distributions such as adsorption profiles at walls or the free interface between a protein-rich and a protein-poor phase. This can be done either in the framework of classical density functional theory, which allows one to determine density distributions and thermodynamic quantities on equal footing, or with the help of computer simulations.

Methods

Bonding probability from Wertheim theory for patchy particles. The basic result of the Wertheim theory is the bonding probability p_b from which the free energy and other properties can be calculated. The bonding probability for m similar patches follows from the mass-action equation^{14,44}

$$\frac{p_b}{(1-p_b)^2} = \rho m \Delta_{ij} \quad (9)$$

$$\Delta_{ij} = 4\pi \int_0^\infty g_{HS}(R_{12}) \langle f_{ij}(1,2) \rangle R_{12}^2 dR_{12}. \quad (10)$$

$\langle f_{ij}(1,2) \rangle$ denotes the average of the Mayer function $f_{ij}(1,2) = \exp(-\beta V(1,2)) - 1$ over all relative orientations of the two particles at fixed distance R_{12} . For very short-ranged square-well attraction one can employ the Carnahan–Starling contact value for the pair correlation function $g_{HS}(\sigma)$ of the hard sphere reference system, in order to approximate Δ_{ij} analytically¹.

Choice of model parameters. For our calculations we set the number of patches $m = 4$, according to the number of ion bridges per monomer in the protein crystal. The centers of the patches are located within the particle at a distance $d = 0.9 R_p$ from the particle center. $R_p = 3.6$ nm corresponds to the effective sphere radius⁴⁶. For the range of the attractive interaction we choose $r_c = 0.33 R_p$, which is sufficiently smaller than the maximum attraction range for our parameter choices

$$r_c^{(\max)} = \sqrt{d^2 - 2\sqrt{3}dR_p + 4R_p^2} - d \approx 0.40R_p, \quad (11)$$

for which hard core repulsion still ensures the condition of only one bond per patch as required for the Wertheim approach.

The ratio between the ion and protein radii is $R_s/R_p = 1/18$. The bridge energy $\beta\epsilon_{uo} = 14$ and binding energy $\beta\epsilon_b = -5$ are chosen inspired by the experimental behavior of human serum albumin (HSA) and YCl_3 (cf. the Langmuir isotherm $Q = Q_0 + 3N\Theta$ with $N = 6.8$, $Q_0 = -4.4$ and $\beta\epsilon_b = -5.9$ in Fig. 1A).

Free energy of liquid phase. The free energy density of the patch bonds between the particles is given by^{14,44}:



$$\beta f_{\text{bond}} = m \rho \left(\ln(1 - p_b) + \frac{1}{2} p_b \right) \quad (12)$$

with the particle number density $\rho = N/V$. Both the chemical potential μ and the pressure P of the patchy particles consist of the reference part from the hard sphere system and a part arising from the patch attraction:

$$\beta \mu = \frac{\eta(8 + 3(\eta - 3)\eta)}{(1 - \eta)^3} + \ln[\eta] + \beta \frac{\partial f_{\text{bond}}}{\partial \rho}, \quad (13)$$

$$\beta P = \rho \frac{1 + \eta + \eta^2 - \eta^3}{(1 - \eta)^3} + \rho \beta \frac{\partial f_{\text{bond}}}{\partial \rho} - \beta f_{\text{bond}}. \quad (14)$$

Free energy of solid phase. For the solid phase, we used a cell model assuming that all m bonds are formed in a crystal¹¹. The free energy density $f_c(\rho)$ is calculated from the restricted volume for free motion V_{free} in radial and angular direction at particle distance r^{11} :

$$f_c(\rho) = -\rho \log \left[V_{\text{free}} \left(R_p \left(\frac{\rho_c}{\rho} \right)^{1/3} \right) \right] - \rho \frac{m}{2} \epsilon_{pp}, \quad (15)$$

$$V_{\text{free}}(r) = -4 \frac{(r - R_p)(r - d - r_c) r_c^2 - (r - d)^2}{(d + r_c - R_p) R_p R_p^2}. \quad (16)$$

The density ρ_c is given by the volume fraction of a simple cubic crystal $\eta_c = \pi/6 = \rho_c R_p^3 4\pi/3$.

- Jackson, G., Chapman, W. G. & Gubbins, K. E. Phase equilibria of associating fluids. *Mol. Phys.* **65**, 1–31 (1988).
- Chapman, W. G., Jackson, G. & Gubbins, K. E. Phase equilibria of associating fluids. *Mol. Phys.* **65**, 1057–1079 (1988).
- Wertheim, M. Fluids with highly directional attractive forces. I. Statistical thermodynamics. *J. Stat. Phys.* **35**, 19–34 (1984).
- Wertheim, M. Fluids with highly directional attractive forces. II. Thermodynamic perturbation theory and integral equations. *J. Stat. Phys.* **35**, 35–47 (1984).
- Wertheim, M. Fluids with highly directional attractive forces. III. Multiple attraction sites. *J. Stat. Phys.* **42**, 459–476 (1986).
- Wertheim, M. Fluids with highly directional attractive forces. IV. Equilibrium polymerization. *J. Stat. Phys.* **42**, 477–492 (1986).
- Bianchi, E., Largo, J., Tartaglia, P., Zaccarelli, E. & Sciortino, F. Phase diagram of patchy colloids: Towards empty liquids. *Phys. Rev. Lett.* **97**, 168301 (2006).
- Russo, J., Tavares, J. M., Teixeira, P. I. C., Telo da Gama, M. M. & Sciortino, F. Reentrant phase diagram of network fluids. *Phys. Rev. Lett.* **106**, 085703 (2011).
- Whitelam, S. Control of pathways and yields of protein crystallization through the interplay of nonspecific and specific attractions. *Phys. Rev. Lett.* **105**, 088102 (2010).
- Fusco, D. & Charbonneau, P. Crystallization of asymmetric patchy models for globular proteins in solution. *Phys. Rev. E* **88**, 012721 (2013).
- Sear, R. P. Phase behavior of a simple model of globular proteins. *J. Chem. Phys.* **111**, 4800–4806 (1999).
- Kern, N. & Frenkel, D. Fluid–fluid coexistence in colloidal systems with short-ranged strongly directional attraction. *J. Chem. Phys.* **118**, 9882–9889 (2003).
- Gögelein, C. *et al.* A simple patchy colloid model for the phase behavior of lysozyme dispersions. *J. Chem. Phys.* **129**, 085102 (2008).
- Whitelam, S. Nonclassical assembly pathways of anisotropic particles. *J. Chem. Phys.* **132**, 194901 (2010).
- Haxton, T. K. & Whitelam, S. Design rules for the self-assembly of a protein crystal. *Soft Matter* **8**, 3558–3562 (2012).
- Bianchi, E., Blaak, R. & Likos, C. N. Patchy colloids: state of the art and perspectives. *Phys. Chem. Chem. Phys.* **13**, 6397–6410 (2011).
- McManus, J. J. *et al.* Altered phase diagram due to a single point mutation in human γ D-crystallin. *Proc. Natl. Acad. Sci. USA* **104**, 16856–16861 (2007).
- Buell, A. K. *et al.* Position-dependent electrostatic protection against protein aggregation. *ChemBioChem* **10**, 1309–1312 (2009).
- Fusco, D., Headd, J. J., De Simone, A., Wang, J. & Charbonneau, P. Characterizing protein crystal contacts and their role in crystallization: rubredoxin as a case study. *Soft Matter* **10**, 290–302 (2014).
- Harding, M. M. Geometry of metal–ligand interactions in proteins. *Acta Crystallogr., Sect. D* **57**, 401–411 (2001).
- Yamashita, M. M., Wesson, L., Eisenman, G. & Eisenberg, D. Where metal ions bind in proteins. *Proc. Natl. Acad. Sci. USA* **87**, 5648–5652 (1990).
- Zhang, F. *et al.* Reentrant condensation of proteins in solution induced by multivalent counterions. *Phys. Rev. Lett.* **101**, 148101 (2008).
- Roosen-Runge, F., Heck, B. S., Zhang, F., Kohlbacher, O. & Schreiber, F. Interplay of pH and binding of multivalent metal ions: Charge inversion and reentrant condensation in protein solutions. *J. Phys. Chem. B* **117**, 5777–5787 (2013).

- Zhang, F., Zocher, G., Sauter, A., Stehle, T. & Schreiber, F. Novel approach to controlled protein crystallization through ligandation of yttrium cations. *J. Appl. Cryst.* **44**, 755–762 (2011).
- Zhang, F. *et al.* Universality of protein reentrant condensation in solution induced by multivalent metal ions. *Proteins* **78**, 3450–3457 (2010).
- Thomson, J. A., Schurtenberger, P., Thurston, G. M. & Benedek, G. B. Binary liquid phase separation and critical phenomena in a protein/water solution. *Proc. Natl. Acad. Sci. USA* **84**, 7079–7083 (1987).
- Asherie, N. R., Lomakin, A. & Benedek, G. B. Phase diagram of colloidal solutions. *Phys. Rev. Lett.* **77**, 4832–4835 (1996).
- Muschol, M. & Rosenberger, F. Liquid–liquid phase separation in supersaturated lysozyme solutions and associated precipitate formation/crystallization. *J. Chem. Phys.* **107**, 1953–1962 (1997).
- Annunziata, O., Ogun, O. & Benedek, G. B. Observation of liquid–liquid phase separation for eye lens γ S-crystallin. *Proc. Natl. Acad. Sci. USA* **100**, 970–974 (2003).
- Wentzel, N. & Gunton, J. D. Liquid–liquid coexistence surface for lysozyme: Role of salt type and salt concentration. *J. Phys. Chem. B* **111**, 1478–1481 (2007).
- Möller, J. *et al.* Reentrant liquid–liquid phase separation in protein solutions at elevated hydrostatic pressures. *Phys. Rev. Lett.* **112**, 028101 (2014).
- Wolde, P. R. t. & Frenkel, D. Enhancement of protein crystal nucleation by critical density fluctuations. *Science* **277**, 1975–1978 (1997).
- Galkin, O. & Vekilov, P. G. Control of protein crystal nucleation around the metastable liquid–liquid phase boundary. *Proc. Natl. Acad. Sci. USA* **97**, 6277–6281 (2000).
- Stradner, A. *et al.* Equilibrium cluster formation in concentrated protein solutions and colloids. *Nature* **432**, 492–495 (2004).
- Groenewold, J. & Kegel, W. K. Anomalously large equilibrium clusters of colloids. *J. Phys. Chem. B* **105**, 11702–11709 (2001).
- Campbell, A. L., Anderson, V. J., van Duijneveldt, J. S. & Bartlett, P. Dynamical arrest in attractive colloids: The effect of long-range repulsion. *Phys. Rev. Lett.* **94**, 208301 (2005).
- Sator, N. Clusters in simple fluids. *Phys. Rep.* **376**, 1–39 (2003).
- Campi, X., Krivine, H. & Krivine, J. Clustering and thermodynamics in the lattice-gas model. *Physica A* **320**, 41–50 (2003).
- Zhang, F. *et al.* Charge-controlled metastable liquid–liquid phase separation in protein solutions as a universal pathway towards crystallization. *Soft Matter* **8**, 1313–1316 (2012).
- Zhang, F. *et al.* The role of cluster formation and metastable liquid–liquid phase separation in protein crystallization. *Faraday Discuss.* **159**, 313–325 (2012).
- Roth, R., Evans, R. & Louis, A. A. Theory of asymmetric nonadditive binary hard-sphere mixtures. *Phys. Rev. E* **64**, 051202 (2001).
- Noro, M. G. & Frenkel, D. Extended corresponding-states behavior for particles with variable range attractions. *J. Chem. Phys.* **113**, 2941–2944 (2000).
- Flory, P. J. Molecular size distribution in three dimensional polymers. I. gelation. *J. Am. Chem. Soc.* **63**, 3083–3090 (1941).
- Bianchi, E., Tartaglia, P., Zaccarelli, E. & Sciortino, F. Theoretical and numerical study of the phase diagram of patchy colloids: Ordered and disordered patch arrangements. *J. Chem. Phys.* **128**, 144504 (2008).
- Soraru, D. *et al.* Protein cluster formation in aqueous solution in the presence of multivalent metal ions – a light scattering study. *Soft Matter* **10**, 894–902 (2014).
- Roosen-Runge, F. *et al.* Protein self-diffusion in crowded solutions. *Proc. Natl. Acad. Sci. USA* **108**, 11815–11820 (2011).

Acknowledgments

We thank Martin Oettel and Hendrik Hansen-Goos (both University of Tübingen) for stimulating discussions on the manuscript. F.R.-R. acknowledges a fellowship of the Studienstiftung des deutschen Volkes. The work was supported by the DFG.

Author contributions

F.R.-R., F.Z., F.S. and R.R. designed the research. F.R.-R. and R.R. performed the calculations and analyzed data. F.R.-R. prepared all figures. F.R.-R., F.S. and R.R. wrote the paper. F.R.-R., F.Z., F.S. and R.R. reviewed the manuscript.

Additional information

Competing financial interests: The authors declare no competing financial interests.

How to cite this article: Roosen-Runge, F., Zhang, F., Schreiber, F. & Roth, R. Ion-activated attractive patches as a mechanism for controlled protein interactions. *Sci. Rep.* **4**, 7016; DOI:10.1038/srep07016 (2014).



This work is licensed under a Creative Commons Attribution-NonCommercial-NoDerivs 4.0 International License. The images or other third party material in this article are included in the article's Creative Commons license, unless indicated otherwise in the credit line; if the material is not included under the Creative Commons license, users will need to obtain permission from the license holder in order to reproduce the material. To view a copy of this license, visit <http://creativecommons.org/licenses/by-nc-nd/4.0/>