Kinetics of Network Formation and Heterogeneous Dynamics of an Egg White Gel Revealed by Coherent X-Ray Scattering

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The kinetics of heat-induced gelation and the microscopic dynamics of a hen egg white gel are probed using x-ray photon correlation spectroscopy along with ultrasmall-angle x-ray scattering. The kinetics of structural growth reveals a reaction-limited aggregation process with a gel fractal dimension of $\approx 2$ and an average network mesh size of ca. 400 nm. The dynamics probed at these length scales reveals an exponential growth of the characteristic relaxation times followed by an intriguing steady state in combination with a compressed exponential correlation function and a temporal heterogeneity. The degree of heterogeneity increases with decreasing length scale. We discuss our results in the broader context of experiments and models describing attractive colloidal gels.

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Egg white, apart from being a major protein source in our daily diet, is one of the most versatile products in the food industry due to its multifunctional properties such as foaming, emulsifying, and gelling [1–5]. Gelation of proteins [6], especially as a result of heat-induced denaturation, leads to a three-dimensional network structure through the formation of disulfide cross-links and hydrogen bonds [1,7,8]. While various experiments mainly focused on the understanding of structural evolution at the molecular level [1,9], the corresponding evolution of the microscopic dynamics in a heat-treated protein gel has not been fully explored yet.

So far, the studies of the dynamic properties of thermal gels of proteins have only contributed to the understanding of internal or short-time self-diffusion processes in protein systems occurring at nanosecond and subnanosecond timescales [10,11]. However, the process of protein gelation involves rather a hierarchy of length and timescales. This requires the understanding of the structure and dynamics of protein gels on length scales ranging from single proteins up to the network mesh size (hundreds of nanometers to micrometers), and timescales of milliseconds to hundreds of seconds. This constitutes a considerable challenge both for simulations and experiments with the need to capture especially nonequilibrium phenomena such as aging and dynamical heterogeneity.

Applying state-of-the-art low-dose x-ray photon correlation spectroscopy (XPCS) along with ultrasmall-angle x-ray scattering (USAXS), we follow here the simultaneous evolution of the microscopic dynamics on length scales of the network mesh size and the structural evolution corresponding to the gelation kinetics of hen egg white. We show that, under the chosen conditions, the kinetic evolution of the gel network can be remarkably well separated from the dynamics. We find that the gel exhibits stress-activated dynamics with an exponential rise of the relaxation time (aging) and a subsequent steady-state ballistic motion displaying significant temporal heterogeneity. Our experiments show that the dynamical aging sets in at timescales well beyond the formation time of the network structure. We identify the stress-driven dynamics as dynamical rupture events which do not change the structure of the gel. The spatial extension of these decorrelation events decreases from 100 nm to a few nm upon aging accompanied by a lowering of the degree of dynamical heterogeneity.

The hen egg sample was purchased from a supermarket. The egg white was extracted in the laboratory, filled in quartz capillaries with a diameter of 1.5 mm, sealed with parafilm, and mounted on a sample stage equipped with a temperature-controlled heating stage (Linkam Scientific Instruments Ltd., UK) to perform XPCS experiments in USAXS geometry [12,13] at the beam line P10 of PETRA III (DESY, Hamburg, Germany, with $\lambda = 1.54 \, \text{Å}$) [14]. Applying a large beam size of $100 \times 100 \, \mu\text{m}^2$ allowed us to perform the experiment at x-ray doses below the damage threshold. We recorded a series of time-resolved scattering patterns (with a temporal resolution of 40 ms) using an area detector, Eiger X 4M ($75 \times 75 \, \mu\text{m}^2$ pixel size) mounted 21.3 m downstream of the sample (details in the Supplemental Material [15]).

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sulfhydryl (SH) groups [7,20]. This, in turn, reduces facilitates an enhanced exposure of the hydrophobic and unfold and assume a different conformational state, which [15] of the measurements indicates a structural evolution in the first 160 s [see Fig. S2(a) in the Supplemental Material [15]]. During this step, major protein components unfold and assume a different conformational state, which facilitates an enhanced exposure of the hydrophobic and sulphydryl (SH) groups [7,20]. This, in turn, reduces α-helix structures and increases β-sheet components [7,22]. The rate of increase in intensity in the USAXS profiles reduces with time [see Figs. S2(b) and S2(c) in the Supplemental Material [15]] and eventually stabilizes, showing no further structural change within the measured q range. The stabilization of I(q) suggests that the major structural evolution corresponding to the denaturation and formation of the gel network is completed over the measured length scales (∼60–2000 nm).

Next, we calculate the exponent δ of the power law relation of I(q) as a function of q(I(q) ∝ q−δ) [23] in the low q regime (0.0036 – 0.0077 nm−1) to determine a characteristic parameter, the fractal dimension, which indicates the extent of filling of the available space by the structure in question [6,24–26]. δ as a function of tw is shown in Fig. 1(b). δ gradually increases with tw and eventually saturates at a value of ≈ 2 confirming that the present aggregation can be described by the RLA process [19].

We further characterize the development of the characteristic length scale ξ of the gel network and determine the mesh size of the gel in the final stages using the Ornstein-Zernike equation (see the Supplemental Material [15]) [27,28] and shown in Fig. 1(c). The mesh size of the network ξ (after tw ∼ 300 s) asymptotically approaches a value of ca. 400 nm. Note that within a few days of age of the egg, the sample freshness does not alter our result significantly as suggested by the SAXS measurements (see Fig. S4 in the Supplemental Material [15]). We then investigated the dynamics of the gel at the length scales related to such mesh size aiming to understand its relation with the structural evolution.

The evolution of dynamics is obtained from the two-time correlation (TTC) defined as the covariance of the scattered intensity [12,13,29–35]

\[
C_{ij}(q, t_1, t_2) = \frac{\langle I_p(q, t_1)I_p(q, t_2) \rangle_{\text{pixels}}}{\langle I_p(q, t_1) \rangle_{\text{pixels}} \langle I_p(q, t_2) \rangle_{\text{pixels}}},
\]

where \( I_p \) is the intensity at the pixel p, and \( \langle . \rangle_{\text{pixels}} \) indicates an average over the pixels within a given wave vector range \( q \pm \delta q \). \( t_1 \) and \( t_2 \) are the times at which the intensity was measured, \( t_w = (t_1 + t_2)/2 \) is the distance along the diagonal (\( t_1 = t_2 \)), and the time difference \( t = |t_1 - t_2| \) is the distance away from the diagonal (see Fig. S5 in the Supplemental Material [15]) [12,13, 29–37]. During the gelation, we performed five consecutive XPCS runs (each run corresponding to 160 s) at different fresh sample spots, and the corresponding TTC are depicted in Figs. 2(a)–2(c) to follow the evolution throughout the entire measurement time.

In Figs. 2(a)–2(c), a pronounced slowing-down of the dynamics with tw is observed. Note that the dynamics is observable only after 160 s [starting from Fig. 2(b)] when the major part of the structural evolution has taken place [see Figs. 1(a)–1(c)]. The inset in Fig. 2 schematically

![FIG. 1. (a) Invariant as a function of tw calculated over the q range of 0.003 – 0.1 nm−1, showing an exponential growth (red solid line) of aggregates, (b) fractal dimension δ as a function of tw obtained at the low q region of the USAXS profiles, and (c) mesh size, as extracted from Ornstein-Zernike plot, is shown as a function of tw.](image-url)
Fig. S6 in the Supplemental Material [15] as a function of the aging of the gel [39,40]. At a later stage [Figs. 2(d) and 2(e)], the relaxation time stabilizes around a mean value, and interestingly, shows a periodic temporal fluctuation, which is indicative of dynamical heterogeneity.

The observed growth of the dynamics is suggestive of an aging of the gel [39,40]. At a later stage [Figs. 2(d) and 2(e)], the relaxation time stabilizes around a mean value, and interestingly, shows a periodic temporal fluctuation, which is indicative of dynamical heterogeneity.

The relaxation times extracted from the fit of \( g_2(q, t) \) (see Fig. S6 in the Supplemental Material [15]) as a function of \( t_w \) are shown in Fig. 3. As we observe in the TTC, the growth of \( \tau \) starts when the rapid change in structure (in the measured \( q \) range) ends. This observation suggests that the microscopic dynamics during the gelation process (approximately the first 160 s after the heating started) is too fast to be captured within our experimental time window. Thus, the measured dynamics after 160 s of heating, when there are no significant structural changes, could be related to the aging or the stabilization of the networks through local reorganization that occurs in a gel (after the gel formation). The initial rapid increase in \( \tau \) [the orange background in Fig. 3(a)] follows an exponential growth as a function of \( t_w \) [shown by the dashed line in Fig. 3(a)]. This behavior is visible for all the measured \( q \) values [see Fig. 3(a)]. After \( \sim 500 \) s, the dynamics stabilizes [the green background in Fig. 3(a)] at a characteristic time fluctuating around a mean value of a few tens of seconds [ca. \( \tau < 100 \) s; see the inset of Fig. 3(a)]. This observation seems to be unique for the present complex system distinguishing it from conventional colloidal or polymeric gels [41–43].

The stretching exponent \( \gamma \) displays a pronounced dependence on the waiting time evidencing the evolution of the dynamics during gelation. In the early times, we observe an exponential (\( \gamma \approx 1 \)) correlation function. Beginning at \( \sim 300 \) s the values of \( \gamma \) start to increase, reaching values of more than 2 [in Fig. 3(b)] and then fluctuate well above 1 indicating a transition from an exponential to a steeper-than-exponential dynamics [32,43].

More information about the dynamics can be obtained from the \( q \) dependence of \( \gamma \) [see Figs. S8(a)–S8(d) in the Supplemental Material [15]] and \( \tau(q) \) [see Fig. S8(e) in the Supplemental Material [15]]. We observe a strong \( q \) dependence of \( \gamma \) at intermediate waiting times (\( \sim 320–640 \) s). Interestingly, \( \gamma \) shows weak or no \( q \) dependence in the initial waiting times (before 300 s) as well as at the later stages (after 600 s). Figure S8(e) in the Supplemental Material [15] depicts the \( q \) dependence of \( \tau(q) \) modeled with a power law \( [\tau(q) \sim q^{-\alpha}] \). The data indicate \( \alpha \approx 1 \) throughout the measurement time, ruling out Brownian diffusive motion (\( \alpha = 2 \)) of the aggregates. Instead, the data suggest that the particle displacement increases linearly with time, which, in combination with a compressed exponential correlation function \( (\gamma > 1) \), are the signatures of intermittent hyperdiffusive dynamics progressing by a limited number of single decorrelation events [39,41,44,45].

The \( q \) dependence of \( \gamma \) can be understood in the framework of the relaxation of stresses generated during the network formation, i.e., during the random cross-linking. At the early stages, during the establishment of the gel network through cross-linking, the dynamics is nearly exponential [see Figs. 3(a) and 3(b)] [46]. As the sample ages, the increased cross-linking accumulates the stresses in the gel. The relaxation of such trapped stresses through large-scale rearrangements leads to the compressed exponential relaxation [43,46]. We speculate that, at these intermediate stages, the possibility of the inhomogeneous distribution of the stress in space in the cross-linked network leads to the \( q \)-dependent \( \gamma \). As the sample ages further, such inhomogeneity reduces, and thus, the dynamics exhibits \( \gamma \approx 2 \) for the entire \( q \) range.

We further explore the gel dynamics by calculating the average spatial extension \( \sigma \) of the decorrelation events adopting the method described in Refs. [47–50]. Applying this methodology, the intermediate scattering function \( f(t) = \sqrt{g_2(t) - 1} / \beta \) is expressed as a series of decorrelation events of the gel network

\[
f(t) = \sum_{N=0}^{\infty} P_I(N) h(N). \tag{2}
\]

\( P_I(N) \) is the probability of \( N \) events occurring during a time interval \( t \) given by a Poisson distribution.
dynamic susceptibility given by \[12,13,29,39\] system \[12,52\]. We quantified the dynamical heterogeneity indicate the presence of dynamical heterogeneity in the of independent regions in the system and result in discrete spatial correlations of the dynamics that restrict the number temporal modulation. Such fluctuations could occur due to reduced number of small decorrelation events, which leads to a this stiffening, the system relaxes slowly through a larger structure of the gel network facilitates such large rearrangement events. At this stage, the relatively soft and flexible of the system, immediately after gel formation, progresses through a small number of relatively large rearrangement events. With increasing \( t_w \), the network stiffens gradually as indicated by the increase in elastic modulus with time in a colloidal gel \[51\], despite the absence of further structural changes observed in Fig. 1. As a result of this stiffening, the system relaxes slowly through a larger number of small decorrelation events, which leads to a reduced \( \sigma \) and an increased \( \tau \).

We observed in Figs. 2(d) and 2(e) that \( \tau \) exhibits a temporal modulation. Such fluctuations could occur due to spatial correlations of the dynamics that restrict the number of independent regions in the system and result in discrete rearrangement events in the gel. These fluctuations, thus, indicate the presence of dynamical heterogeneity in the system \[12,52\]. We quantified the dynamical heterogeneity by calculating the fourth order correlation function or the dynamic susceptibility given by \[12,13,29,39\]

\[ h(q,N) \approx \exp[-(qN\sigma)^2] \quad (3) \]

for a ballistic motion (i.e., \( \alpha = 1 \)) \[50\]. \( \Gamma_0 \) is kept constant at 0.1 and \( N \) is varied from 0 to 100. With this, we obtain theoretical \( g_2 \) functions yielding values of \( \gamma \) as a function of \( q \sigma \).

The black line in Fig. 4(a) shows \( \gamma \) as a function of \( q \sigma \) extracted from the modeled \( g_2 \) functions. The data super-impose with the black line when the corresponding \( q \) values of the datasets are multiplied by individual values of \( \sigma(t_w) \) for each time interval. Figure 4(b) shows \( \sigma(t_w) \) as a function of \( t_w \) indicating a gradual reduction in \( \sigma \) with increasing \( t_w \). Larger values of \( \sigma \) at earlier times imply that the relaxation of the system, immediately after gel formation, progresses through a small number of relatively large rearrangement events. At this stage, the relatively soft and flexible structure of the gel network facilitates such large restructuring events. With increasing \( t_w \), the network stiffens gradually as indicated by the increase in elastic modulus with time in a colloidal gel \[51\], despite the absence of further structural changes observed in Fig. 1. As a result of this stiffening, the system relaxes slowly through a larger number of small decorrelation events, which leads to a reduced \( \sigma \) and an increased \( \tau \).

Figure 5(a) shows the calculated \( \chi_4 \) as a function of the delay time. The peak position \( \tau^* \) of \( \chi_4 \) corresponds to the characteristic time of the heterogeneous dynamics, while its height \( \chi^* \) gives a measure of the degree of heterogeneity in the dynamics. The extracted \( \chi^* \) and \( \tau^* \) are summarized as a function of \( q \) in Figs. 5(b) and 5(c). Note that the absolute values of \( \tau^* \) do not change significantly with \( t_w \). Nevertheless, the peak height \( \chi^* \) significantly reduces with \( t_w \). It is thus indicating that the degree of heterogeneity reduces with \( t_w \) \[41,48\], possibly through structural rearrangements as the elementary steps along the direction of its equilibrium state. This is in agreement with our observation that the size \( \sigma \) of the restructuring events decreases with \( t_w \) [Fig. 4(b)]. Consequently, the curves of \( \chi^* \) as a function of \( q \sigma \) at different \( t_w \) fall on the same curve [Fig. 5(d)].

The length scale dependence of \( \chi_4 \) reveals that \( \tau^* \) decreases with increasing \( q \) as \( \tau^* \sim 1/q \) [Fig. 5(b)] \[39\] and \( \chi^* \) increases with \( q \) [Fig. 5(c)] \[53\]. The observation of \( \chi^* \) increasing with \( q \) has also been observed previously in attractive colloidal fractal gels \[48\]. In such type of gels, the volume fractions can be very small compared to any noninteracting colloidal gel \[32,54\]. The gelation of the whole egg white where the total volume fraction of proteins is rather low also supports the possibility of such type of dilute colloidal fractal-like gel formation. The gelation of proteins is favored when the electrostatic repulsion between the protein molecules is substantially reduced \[55\]. Our results thus indicate that the electrostatic repulsive forces between the proteins present in their native states in an egg
white are reduced after heat-induced denaturation. Eventually, the system exhibits an interesting attractive colloidal gel-like dynamics. The observed ballistic dynamics ($\tau \sim q^{-1}$) with $\chi^* \sim q$ is possibly due to slow compaction of the gel through discrete rearrangements \cite{48}. At a smaller length scales, especially at the length scales of the mesh size ($\sim 400$ nm and corresponding $q = 0.016$ $\text{nm}^{-1}$), these events might be distinct and observable, which results in higher $\chi^*$ values at smaller length scales (i.e., at higher $q$). On the other hand, while probing at large length scales (i.e., at smaller $q$), the system appears to be rather homogeneous with less temporal fluctuation in the dynamics (i.e., smaller $\chi^*$ values).

To conclude, we simultaneously investigate the kinetics of thermal gelation and dynamics of an egg white gel by employing state-of-the-art XPCS along with USAXS on length scales of the network mesh size. A rapid increase in scattering intensity at the onset of the reaction-limited aggregation process is observed. The microscopic dynamics reveals an exponential rise of the relaxation time and a subsequent steady-state ballistic and heterogeneous dynamics. We discuss the observed dynamics in the framework of a stress-activated ballistic dynamics in a low volume fraction attractive colloidal gel. Our study paves the way for future experiments following protein gelation and aggregation on length scales from nm to microns shedding light on processes highly relevant for the food industry and soft matter physics.

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